

COMPLEMENTARY SUBSPACES:

Let $V(F)$ be a v.s and W_1, W_2 are two subspaces of V . Then W_1, W_2 are said to be complementary subspaces of each others if, $V = W_1 \oplus W_2$

Eg: $W_1 = \{(x, 0, 0) : x \in \mathbb{R}\} < \mathbb{R}^3(\mathbb{R})$. Then what is the complementary subsp. of W_1 ?

Soln: $V = W_1 \oplus W_2$

$$(x, y, z) = (x, 0, 0) + (0, y, z)$$

$$\Rightarrow \exists W_2 = \{(0, y, z) : y \in \mathbb{R}, z \in \mathbb{R}\}$$

*Th. 6 EXISTENCE TH. OF COMPLEMENTARY SUBSPACES.

Let $V(F)$ be a v.s. and $W_1 < V$.

Then $\exists$ a complementary subsp. say W_2 s.t. $V = W_1 \oplus W_2$

COSET OF A SUBGP. IN A GP.

Let $(G, *)$ be a gp. and H be a SUBGP. of G
 Then, for any $a \in G$; $a * H = \{a * h : \forall h \in H\}$
 $= \{a * e, a * h_1, a * h_2, \dots\}$
 $= \text{LEFT COSET.}$

For any, $a \in G$; $H * a = \{h * a : \forall h \in H\}$
 $= \text{RIGHT COSET.}$

- In general; $a * H \neq H * a$
- If G is abelian gp. then $a * H = H * a$